



QUESTION OF THE DAY

Problem: Calculate at what values of x exists relative maxima and/or minima for the function $x^3 - 3x^2 - 14x + 5 = 0$

Solution:

To find the extremes of the function, the critical points must first be found. To find these, set the derivative equal to zero and solve

$$\begin{aligned} \frac{d}{dx} x^3 - 3x^2 - 14x + 5 &= 0 \\ 3x^2 - 6x - 14 &= 0 \end{aligned}$$

Using the Quadratic formula, we can solve for $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$, where $a=3$, $b=-6$, $c=-14$

$$x = \frac{6 \pm \sqrt{6^2 - 4 \cdot 3 \cdot (-14)}}{2 \cdot 3} \Rightarrow x = \frac{3 \pm \sqrt{51}}{3} = 3.3805 \text{ or } -1.3805$$

To find the extrema, plug in the critical points into the second derivative. If it is positive, the graph is concave up and thus the critical point is a minima. If negative, the graph is concave down and thus a max

$$\begin{aligned} \frac{d}{dx} 3x^2 - 6x - 14 \\ 6x - 6 \end{aligned}$$

Thus $6(3.3805) - 6 = 14.283$ which implies that at $x=3.3805$ there is a minimum

Doing the same thing for $x=-1.3805$, $6(-1.3805) - 6 = -14.283$ which implies that at $x=-1.3805$ there is a maximum

At $x = 3.3805$ there is a relative minimum. At $x=-1.3805$ there is a relative maximum
